

A General Purpose Research Simulator (GPRS) for Numerical Simulation On CO₂ Sequestration

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Highlights

- ◆ GPRS is a next-generation research simulator developed in Stanford SUPRI-B group
- ◆ GPRS uses state-of-the-art object-oriented design and is programmed in standard C++
- ◆ GPRS is easy to extend and easy for team development
- ◆ GPRS can be used by multiple researchers with various purposes of reservoir engineering and management
- ◆ Most of SUPRI-B group's research results are tested and reflected in GPRS

Milestones

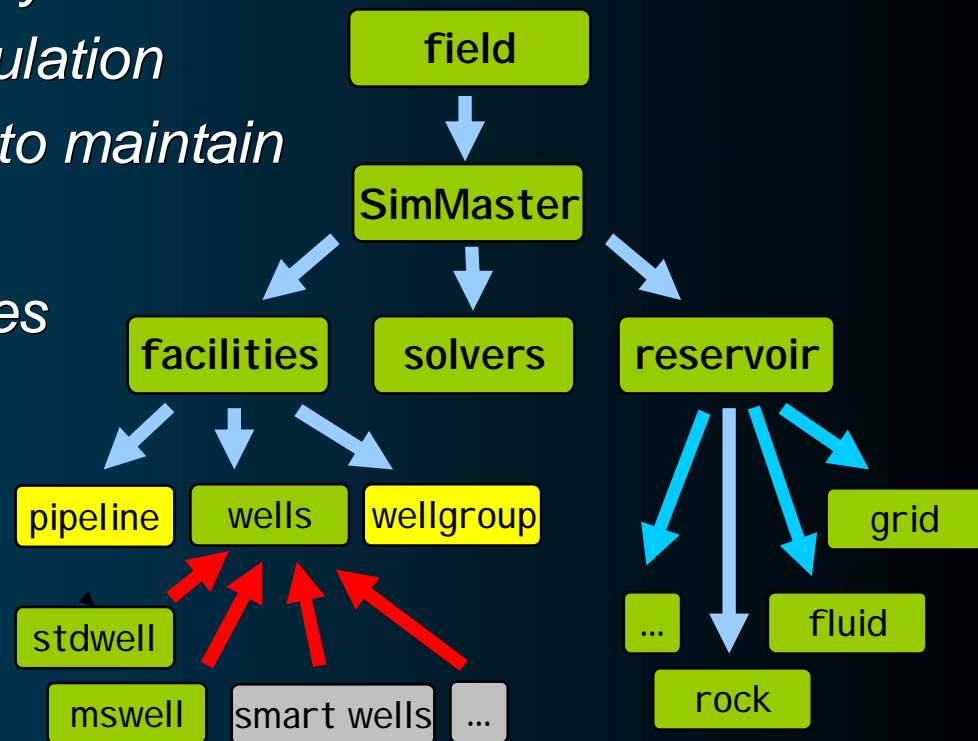
- ◆ **2002:** 1st release of GPRS to SUPRI-B members: generalized unstructured, compositional formulation
- ◆ **2004:** Finished Multi-segment well (MSWell) implementation
- ◆ **2005:** Started to add energy equation; SLB/CVX/Total's Intersect project initiated largely following the philosophy and system design of GPRS
- ◆ **2007:** Finished adding advanced upscaling features for NFR (MSR), conventional reservoirs (ALG), and near-well regions
- ◆ **2009:** Finished generalized chemical-reaction formulation (multi-species)
- ◆ **2010:** Started to implement auto-differential formulation; finished CO₂ sequestration and CBM module; Collaborative development agreement signed between Stanford and Peking University

Features of GPRS

- ◆ State-of-the-Art Object-Oriented Design
- ◆ Full-function Reservoir Simulator
- ◆ Innovative Data Structures
- ◆ Advanced Well Models
- ◆ Compatible with Various Grids
- ◆ Powerful Formulation and Solvers
- ◆ Others

State-of-the-Art Object-oriented Design

- ◆ Major commercial reservoir simulators are still procedure-oriented design (Eclipse, CMG, VIP, etc.)
- ◆ GPRS uses object-oriented design
 - *Much more natural way to model an oilfield*
 - *Enables data-encapsulation*
 - *Clear structure, easy to maintain*
 - *Allow easy teamwork*
 - *Unlimited extensibilities*



Outline

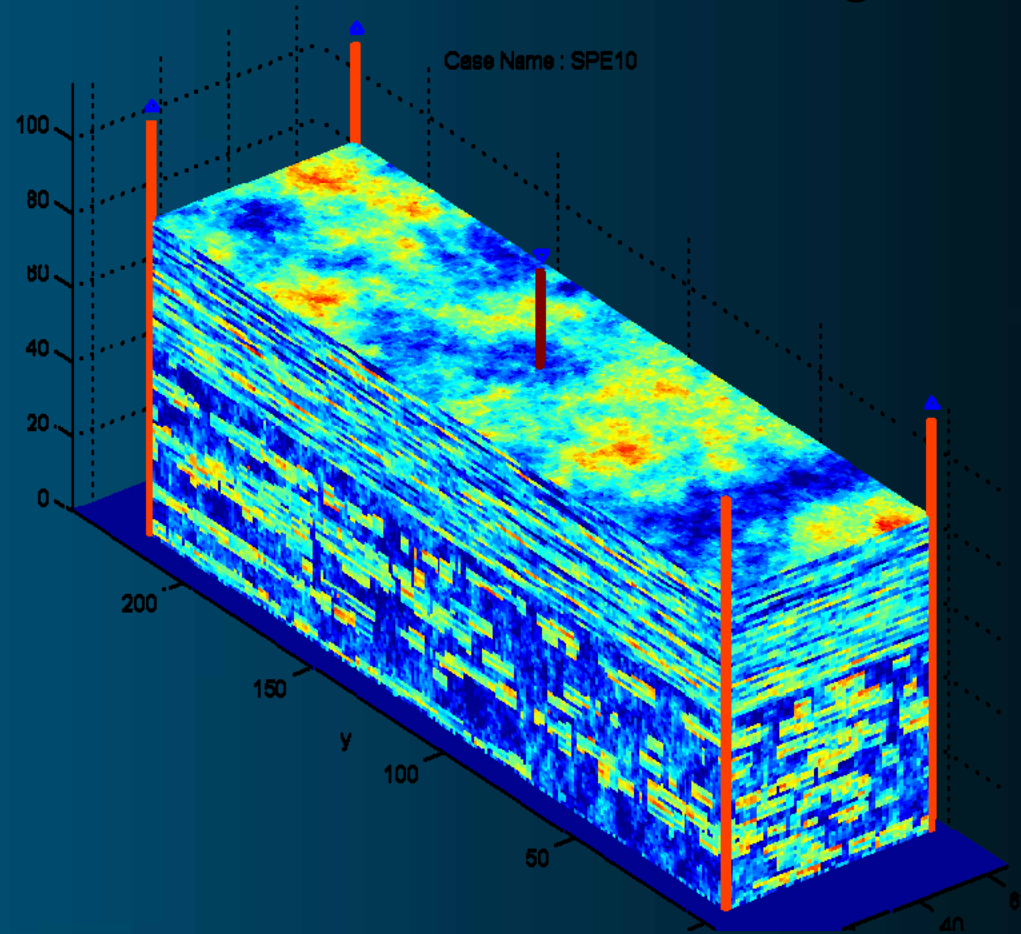
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Full-function Reservoir Simulator

- ◆ A Black-Oil simulator
 - *Allow Any combination of oil-water-gas phases*
 - *A Special case of compositional formulation*
- ◆ A Compositional simulator
 - *Any number of components*
 - *Comprehensive EOS models*
 - *Fast flash calculation*
- ◆ A Chemical-Reaction Simulator
 - *Largely applied in Global Climate and Energy Project (GCEP)'s CCS research*
 - *Ready to use for CBM and Shale Gas simulation*
- ◆ and thermal
 - *On-going work*

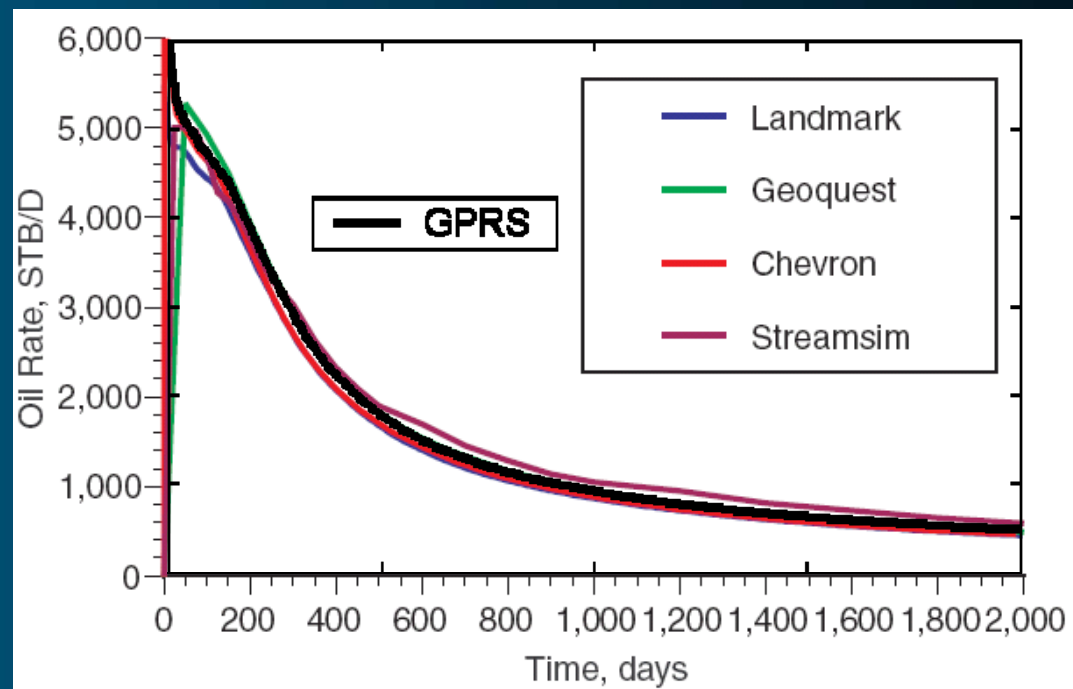
A Black-Oil Example

- ◆ 10th SPE standard comparison project, example 2
- ◆ Oil-water model with 1.12 million grids



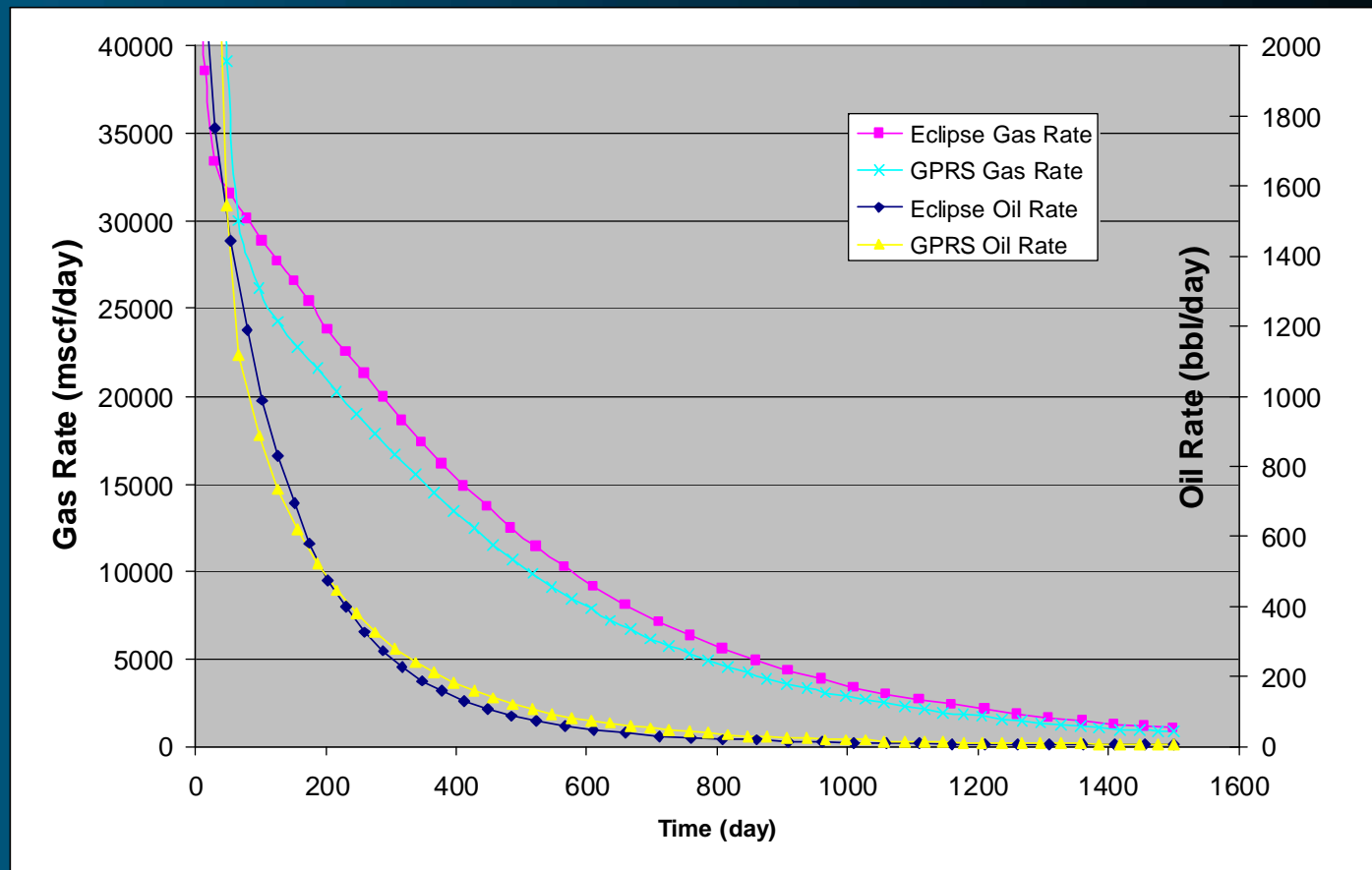
Benchmark Results

- ◆ Matched with industry simulators
- ◆ Much faster than Eclipse
 - It takes GPRS 4.5 hrs on single CPU (2.8GHz)
 - It takes Eclipse 5 hrs on 8 CPUs (2.8 GHz)



A Compositional Example

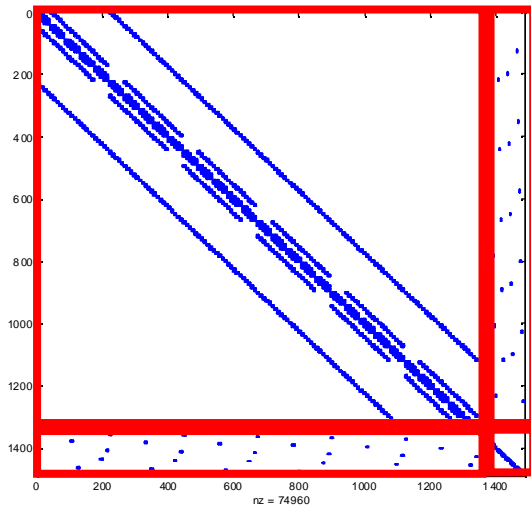
- 3rd SPE standard comparison project
- Gas-Condensate model , 9 HC + water



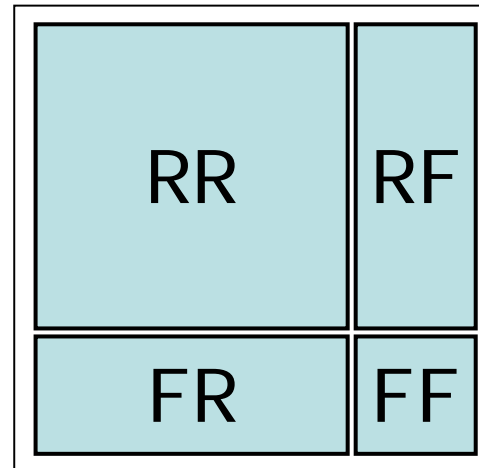
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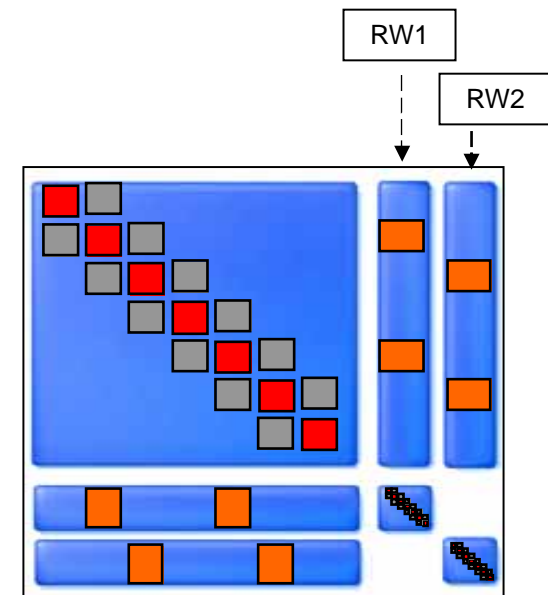
Multi-level Sparse Block Matrix



- ◆ R ~ reservoir
- ◆ F ~ facilities
- ◆ W ~ well

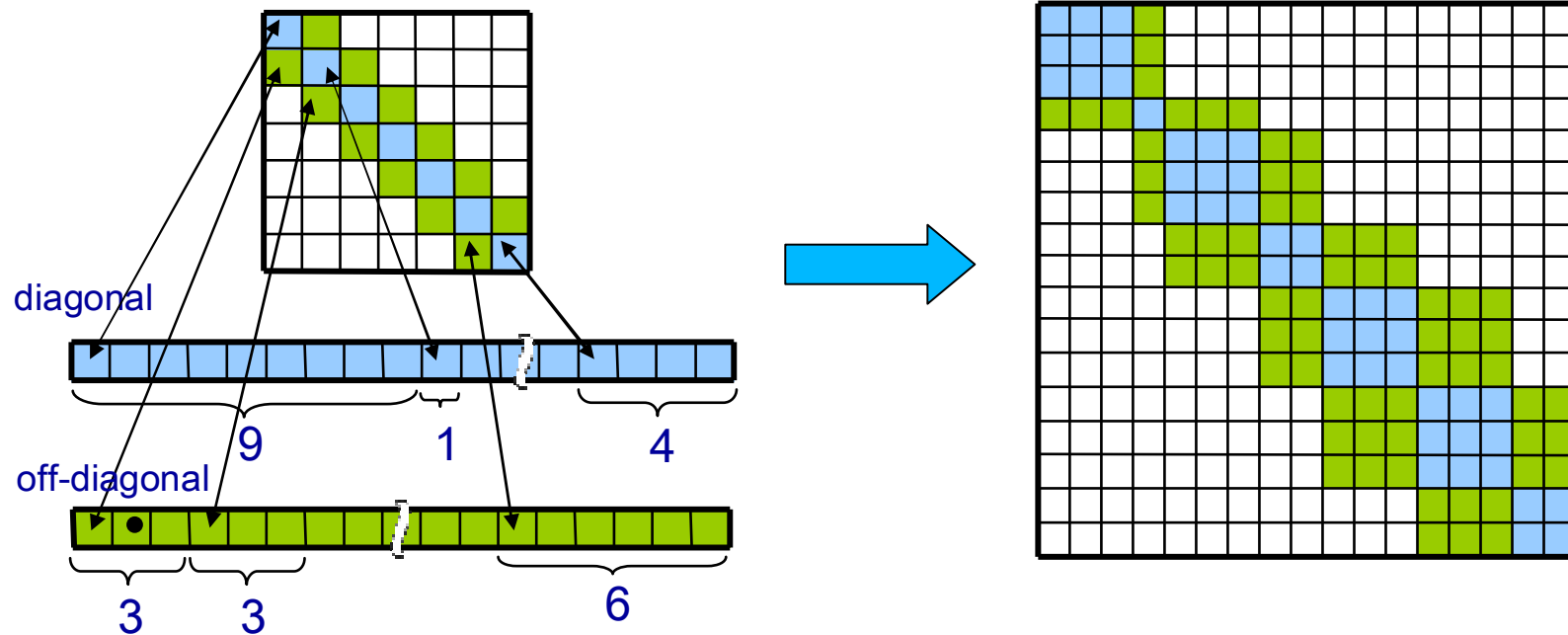


- ◆ Easy to assemble
- ◆ Efficient
- ◆ Extensible



Block Compressed Row Matrix

compressed row sparse pointer matrix



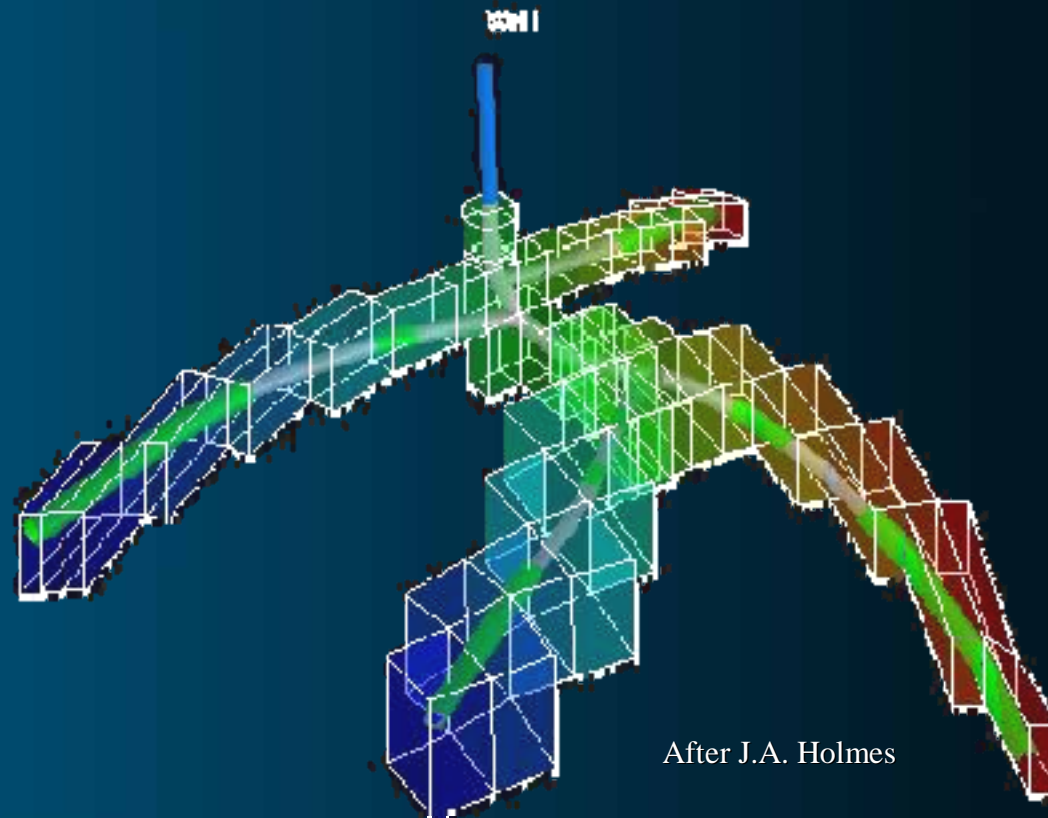
- ◆ Designed specifically for unstructured grid & AIM
- ◆ Easy to adopt new algorithms
- ◆ Better cache utilization

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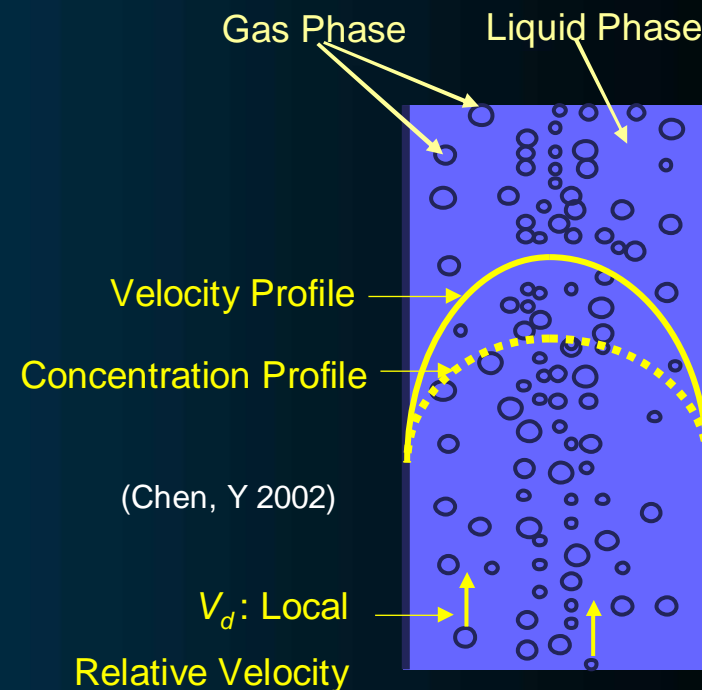
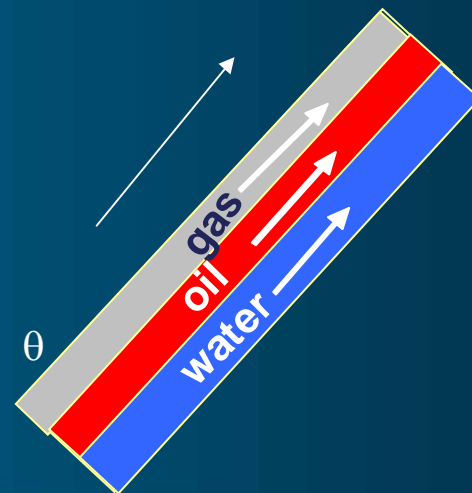
Multi-Segment Well

- ◆ Multi-segment well (MSWell) model describes the flow behavior inside each discretized segment of the wellbore (e.g. J.A. Holmes)

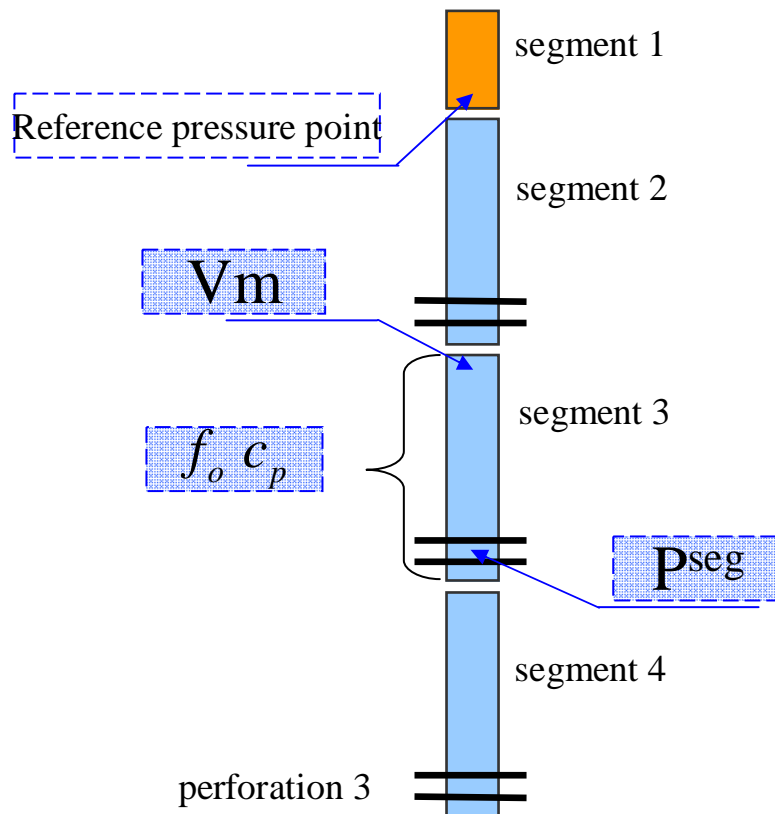


MSWell – More Physics

- ◆ Consider fluid gravity, friction with wellbore, and acceleration
- ◆ Consider the drift-flux between phases
- ◆ Assign variables of pressure, hold-ups, velocity along wellbore



MSWell Formulation



Variables :

P , segment pressure

V_m , mixture velocity

f_o , oil phase hold-up

f_g , gas phase hold-up

Equations:

$$R_{o,i} = (A_i^{n+1} - A_i^n)_o + (F_{i,out}^{seg} - F_{i,in}^{seg})_o - F_{in,o}^{res} = 0$$

$$R_{w,i} = (A_i^{n+1} - A_i^n)_w + (F_{i,out}^{seg} - F_{i,in}^{seg})_w - F_{in,w}^{res} = 0$$

$$R_{g,i} = (A_i^{n+1} - A_i^n)_g + (F_{i,out}^{seg} - F_{i,in}^{seg})_g - F_{in,g}^{res} = 0$$

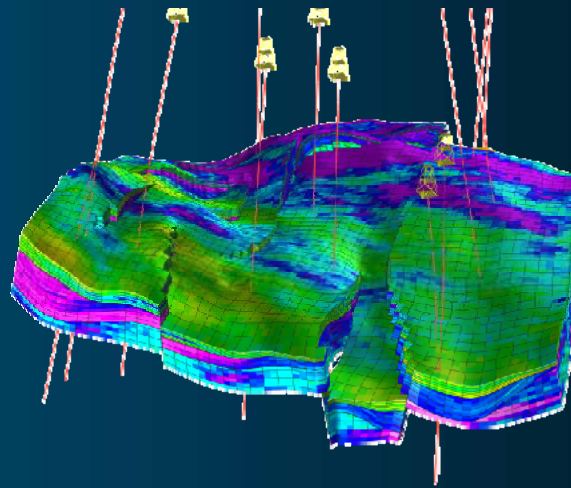
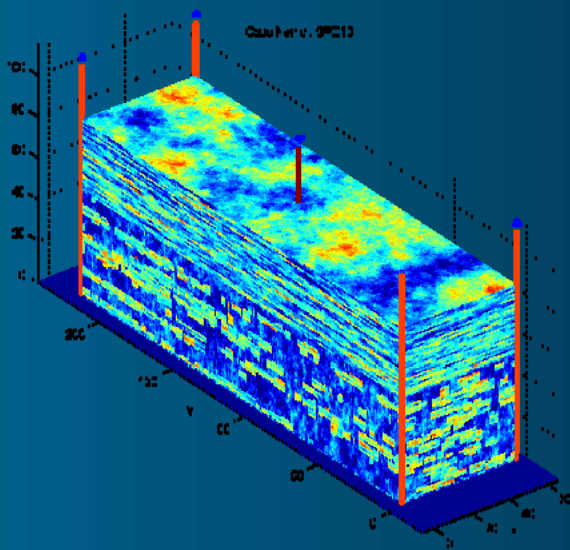
$$\Delta P_{total} = \Delta P_h + \Delta P_f + \Delta P_a$$

Outline

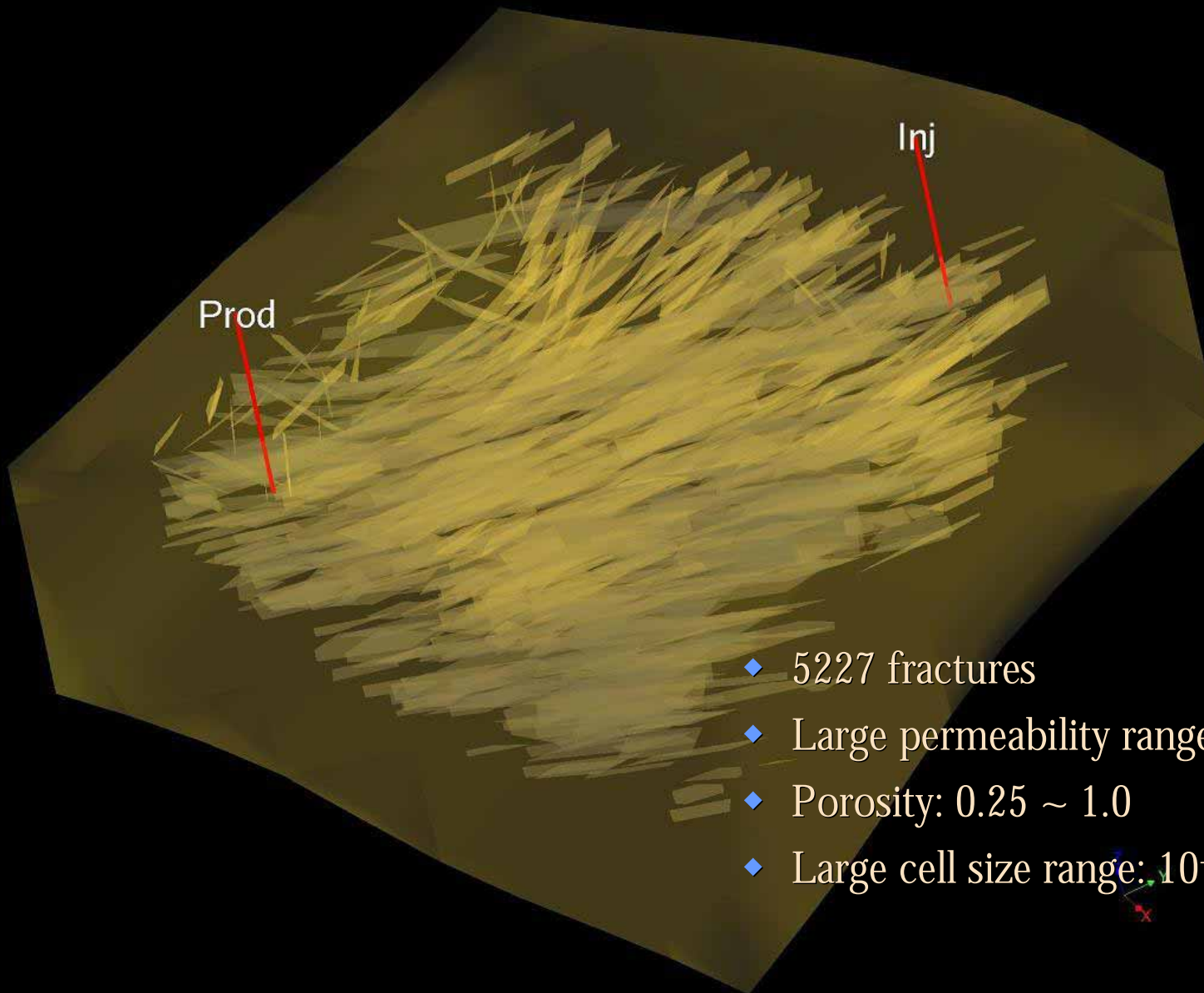
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Grid Types

- ◆ GRPS supports various grid types
 - *Cartesian grid*
 - *Corner-point grid*
 - *Unstructured grid*

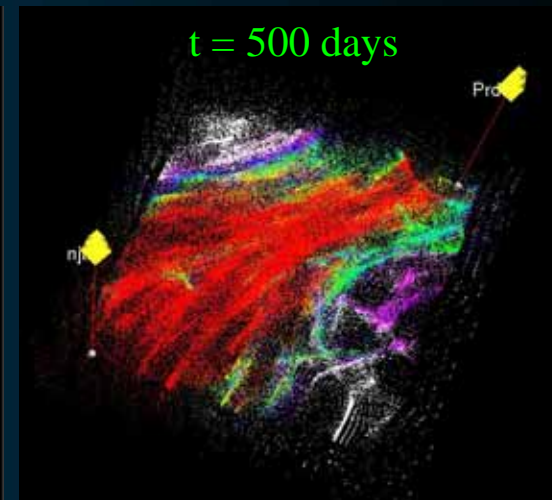
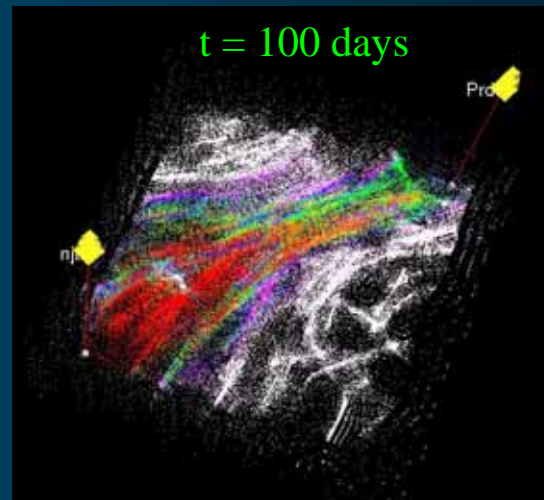
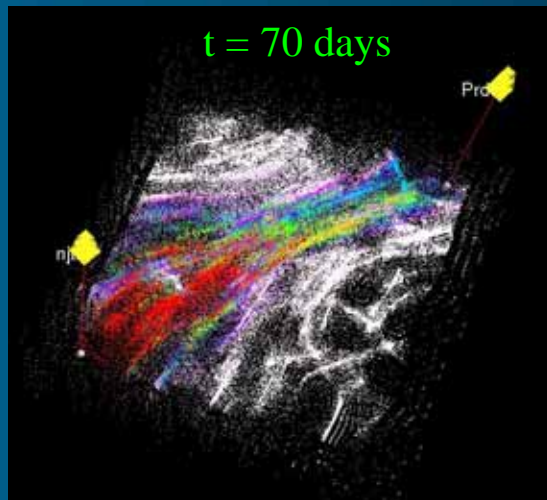
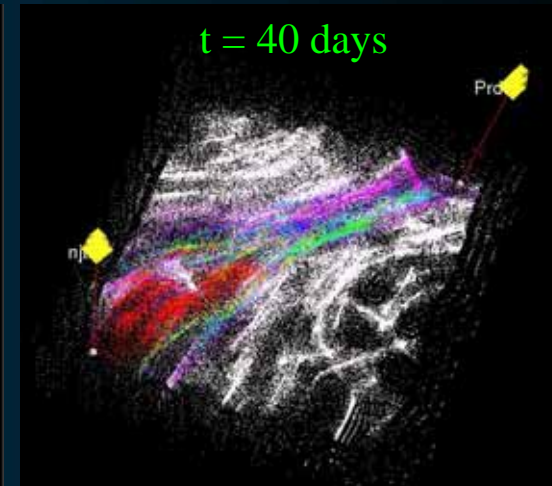
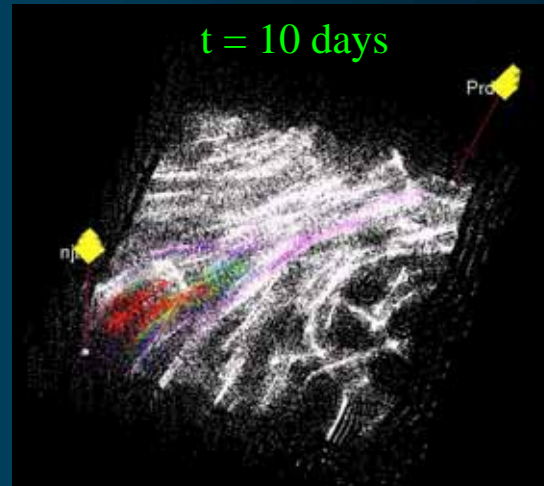
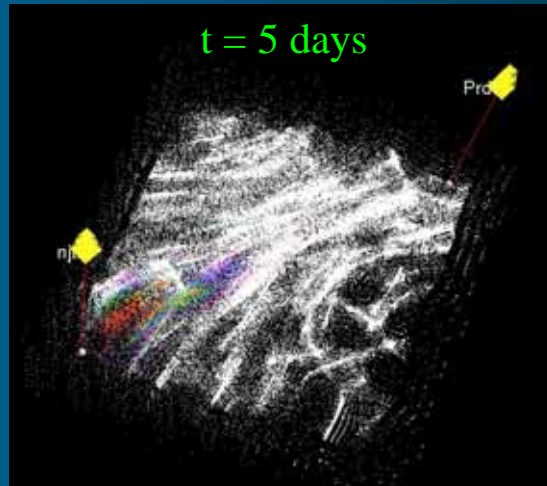


Unstructured Grid Example

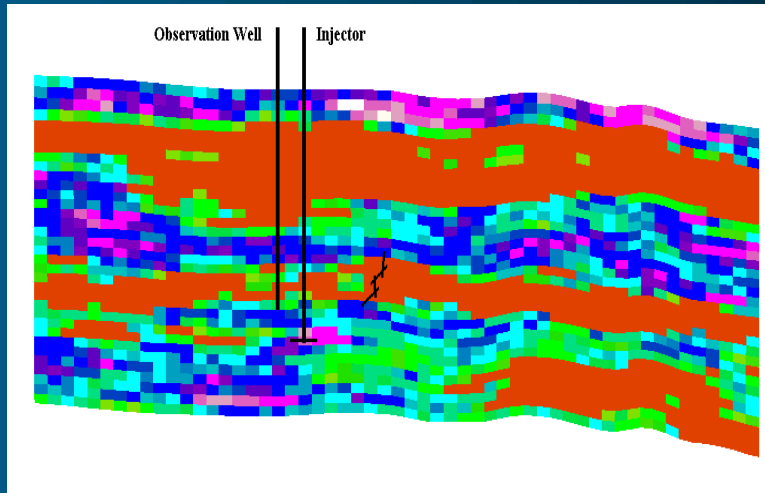


- ◆ 5227 fractures
- ◆ Large permeability range: $0.1 \sim 10^6$ md
- ◆ Porosity: $0.25 \sim 1.0$
- ◆ Large cell size range: $10^{-3} \sim 10^3$ cft

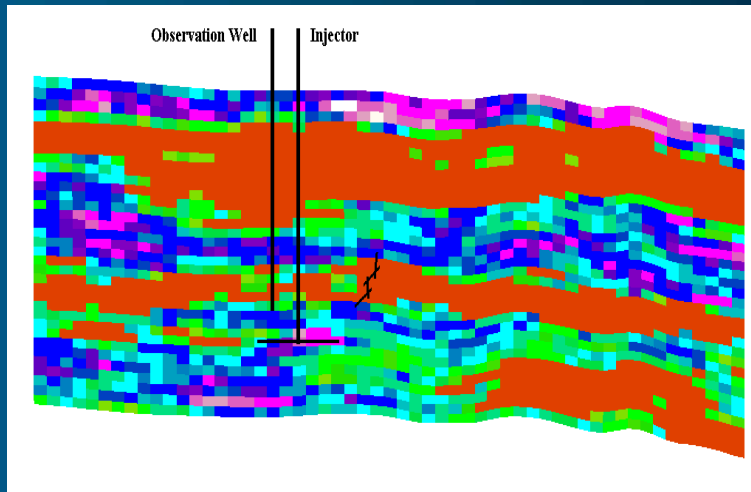
C1 Composition Maps



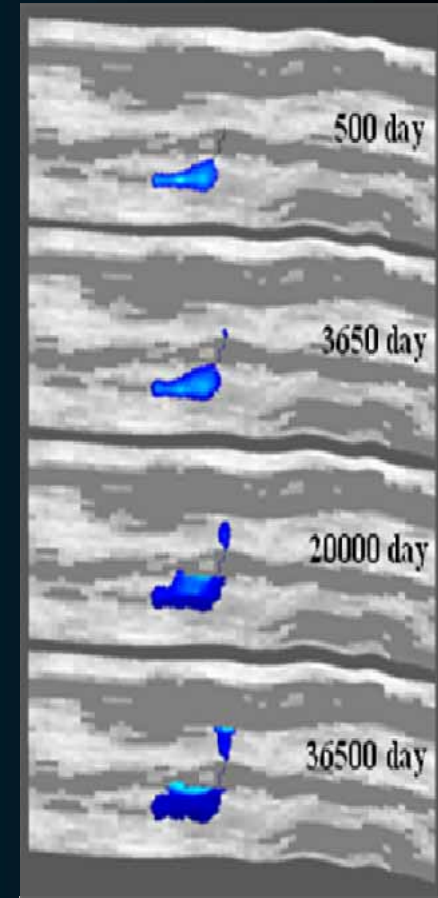
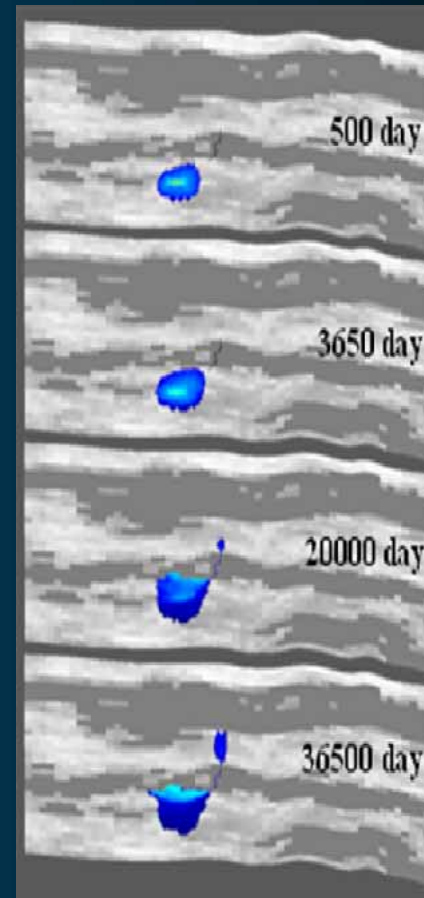
DFM Application in China's First CCS project



Hydraulic Fracture length: 100m



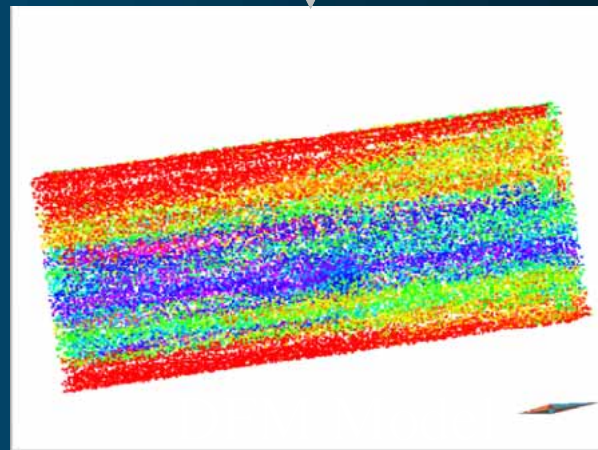
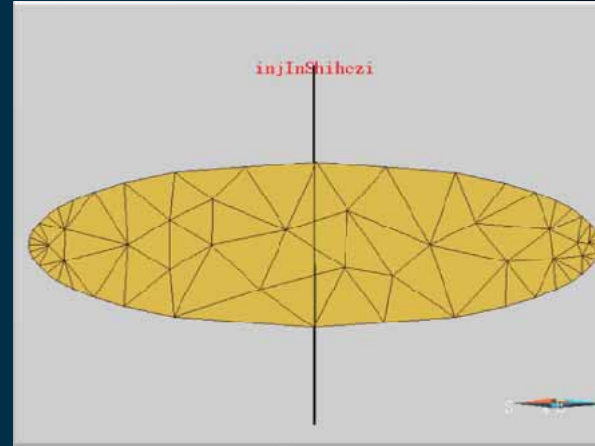
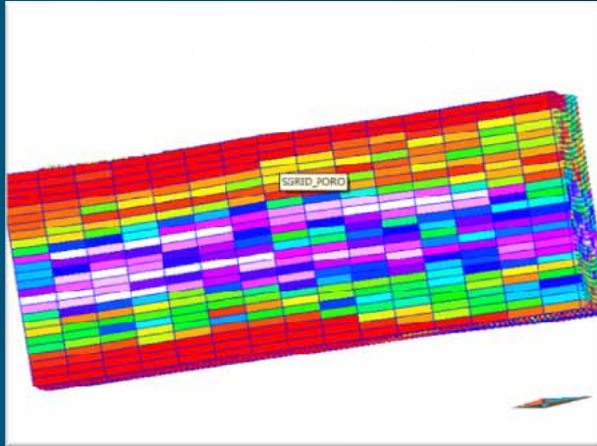
Hydraulic Fracture length: 300m



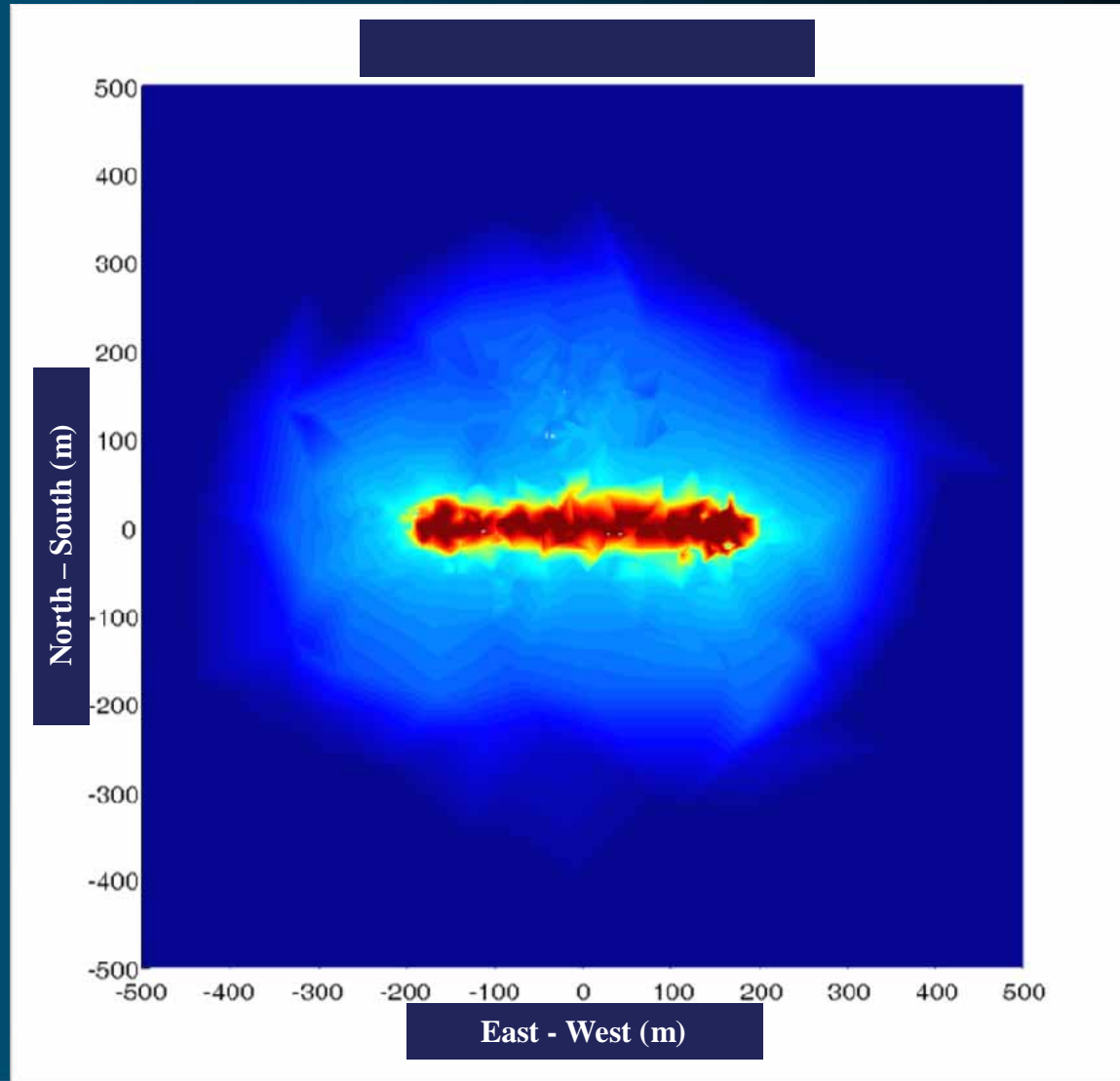
CO2 saturation profiles

3D Model with Hydraulic Fractures

Hydraulic Fracture Model

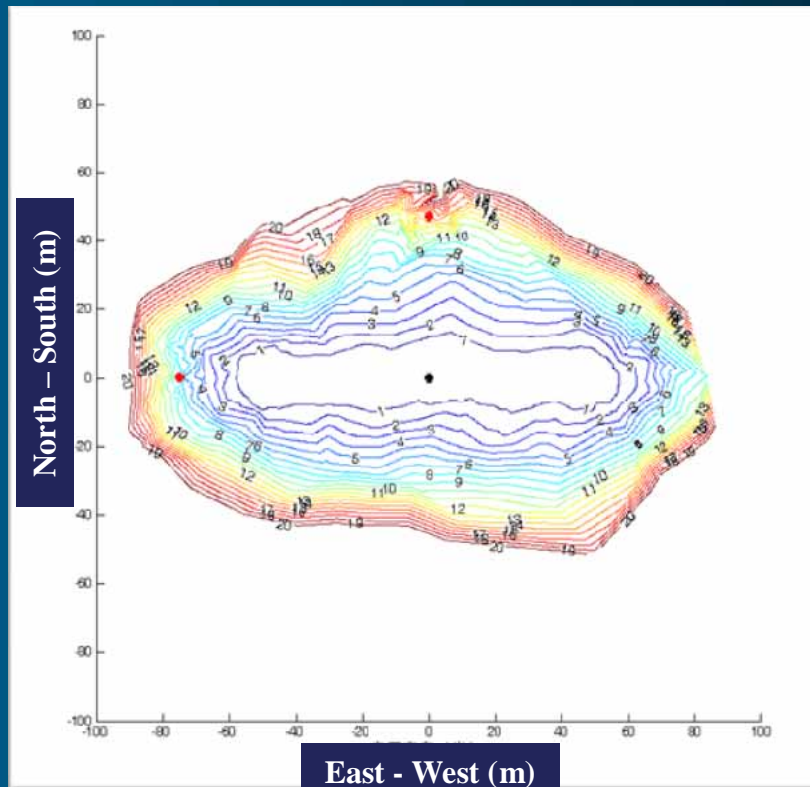


CO₂ Distribution After 5 Years' Injection

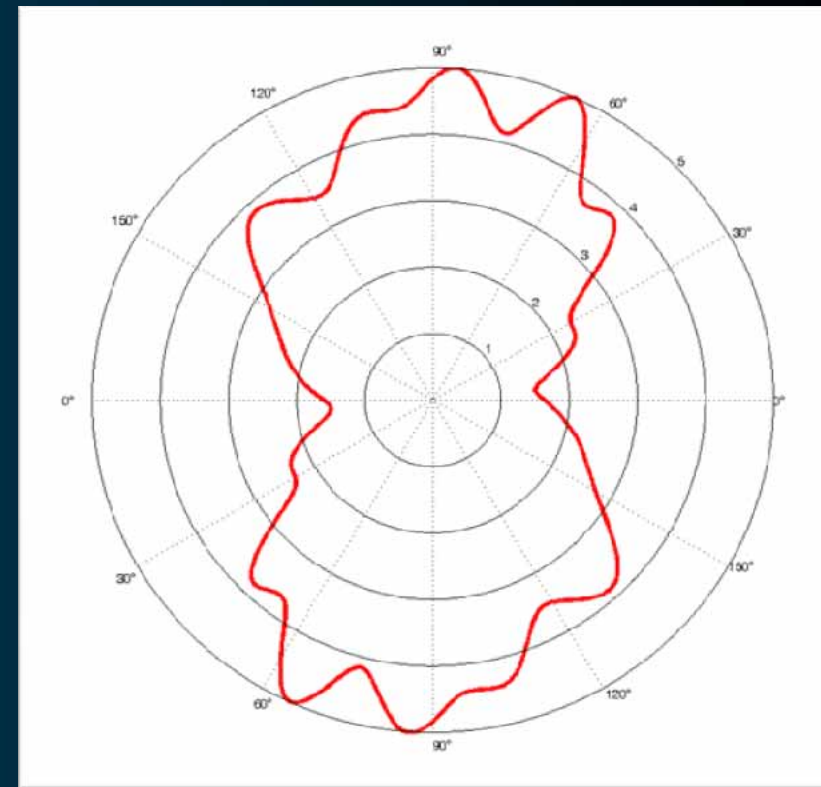


CO₂ Front Observation Time

Time contour map of CO₂ front observation time (month)



CO₂ front observation time at a specific position considering possible fracturing directions (year)



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Powerful Formulations and Solvers

- ◆ GPRS provides more flexible formulations
 - *Fully implicit (FIM) method,*
 - *Implicit pressure explicit saturation (IMPES) method*
 - *Implicit pressure and saturations and explicit component mole fractions (IMPSAT) method*
 - *Adaptive implicit (AIM) method, with any combination of above formulations*

Powerful Formulations and Solvers

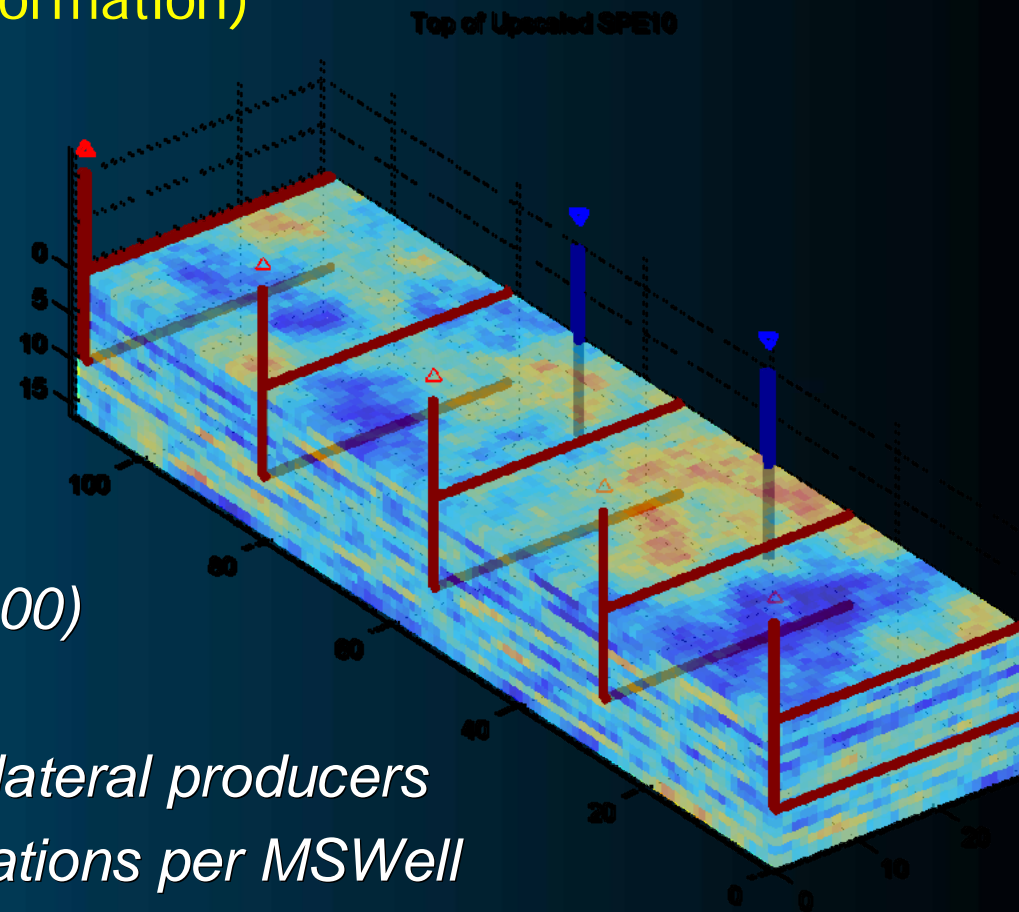
- ◆ GPRS provides a large set of powerful solvers and preconditioners
 - *LAPACK full/banded matrix direct solvers*
 - *BlitzPak iterative solver*
 - *Point-wise / block-wise GMRES iterative solver*
 - *BiCGstab iterative solver*
 - *Point-wise/ block-wise diagonal preconditioners*
 - *Incomplete LU decomposition preconditioners*
 - *Constraint pressure residual (CPR) preconditioners*
 - *AMG preconditioners*

Results

- ◆ CPR method is a two-stage preconditioner
 - *A highly accurate pressure solve as first stage*
 - *A loose ILU global solve as second stage*
- ◆ AIM formulation + block-wise GMRES solver + CPR preconditioner are the best combination for most of reservoir simulation cases
- ◆ Widely recognized by industry

Examples

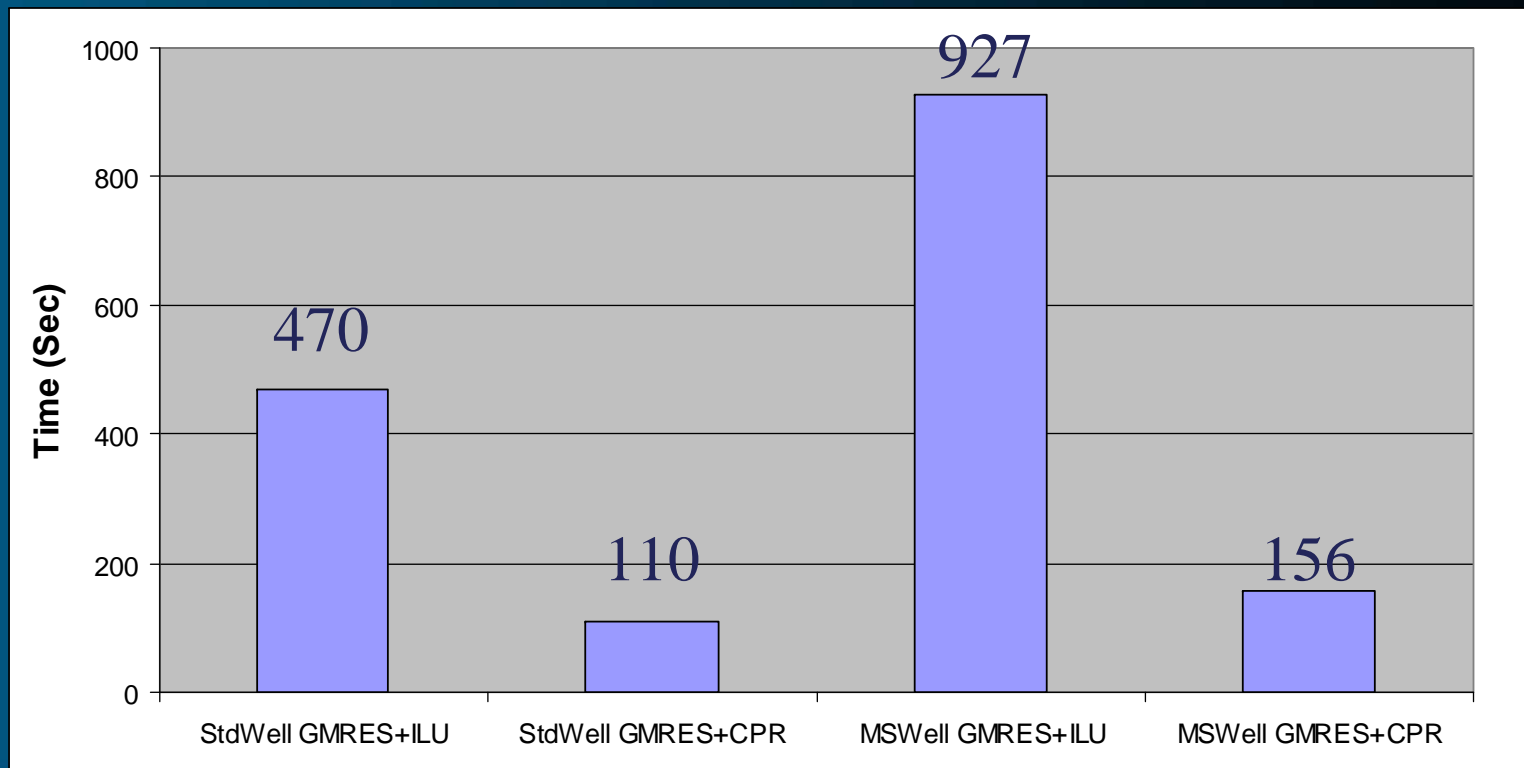
Upscaled SPE10 (top formation)



- *110x30x16 grid (52,800)*
- *Oil-water system*
- *5 multi-segmented bilateral producers*
- *9 segments, 6 perforations per MSWell*
- *2 standard vertical injectors*

Results

- ◆ Two scenarios: producers are modeled with MSWell or not
- ◆ CPR is 4~6 time faster than ILU



Others

- ◆ Programmed in Standard C++, ideally should work on any operating system
- ◆ Currently available in 32-bit/64-bit Windows , Linux and Unix systems

Key Reference

- ◆ H. Cao, *Development of Techniques for General Purpose Simulator*, Ph.D. thesis, Stanford University, 2002
- ◆ Y. Fan, *Chemical Reaction Modeling in a Subsurface Flow Simulator with Application to In-Situ Upgrading and CO₂ Mineralization*, Ph.D. thesis, Stanford University, 2010
- ◆ L.J. Durlofsky, K. Aziz, *Advanced Techniques for Reservoir Simulation and Modeling of Non-conventional Wells*, Final Report to U.S. Department of Energy, contract no. DE-AC26-99BC15213 (2004) 213 pp. 2004

Thank You!



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